

$$(iii) \begin{cases} \vec{R}_1 = (1, 1, -1) \frac{a}{\sqrt{3}} = \vec{R}_2' + \vec{R}_1' - \vec{R}_3' \\ \vec{R}_2 = (1, -1, 1) \frac{a}{\sqrt{3}} = \vec{R}_3' - \vec{R}_2' \\ \vec{R}_3 = (-1, 1, 1) \frac{a}{\sqrt{3}} = \vec{R}_3' - \vec{R}_1' \end{cases}$$

⇒ \vec{R}_1, \vec{R}_2 and \vec{R}_3 can be represented as linear combinations of \vec{R}_1', \vec{R}_2' and \vec{R}_3' .

From (i) and (ii), a lattice point that can be given by linear combinations of \vec{R}_1, \vec{R}_2 and \vec{R}_3 can also be represented as linear combinations of \vec{R}_1', \vec{R}_2' and \vec{R}_3' , and vice versa.

For example, a lattice point $\vec{P} = a_1 \vec{R}_1 + a_2 \vec{R}_2 + a_3 \vec{R}_3 =$
 $a_1 (\vec{R}_2' + \vec{R}_1' - \vec{R}_3') + a_2 (\vec{R}_3' - \vec{R}_2') + a_3 (\vec{R}_3' - \vec{R}_1') =$
 $b_1 \vec{R}_1' + b_2 \vec{R}_2' + b_3 \vec{R}_3'$, with $b_1 = (a_1 - a_3), b_2 = (a_1 - a_2), b_3 = (-a_1 + a_2 + a_3)$

Thus these two lattices are equivalent !!