

1. Packing Fraction

(a) bcc

$$\text{Maximum radius of the sphere} = \frac{\sqrt{3}a}{4}$$

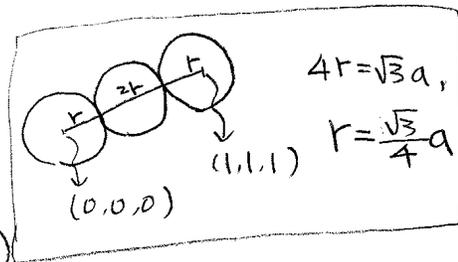
$$\text{Volume of spheres} = \frac{4}{3} \pi r^3 \times \left(1 + \frac{1}{8} \times 8 \right)$$

1 at center

8 on corners

$$= \frac{4}{3} \pi \left(\frac{\sqrt{3}a}{4} \right)^3 \times 2 = \frac{\pi}{8} \sqrt{3} a^3$$

$$\text{Packing Fraction} = \frac{\pi}{8} \sqrt{3} \approx 0.680$$



(b) fcc

$$\text{Maximum radius of the sphere} = \frac{\sqrt{2}a}{4}$$

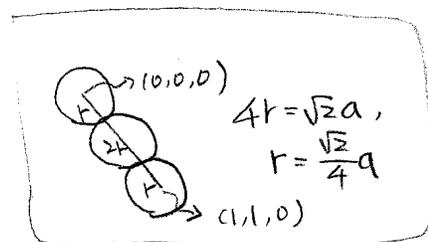
$$\text{Volume of spheres} = \frac{4}{3} \pi r^3 \times \left(\frac{1}{8} \times 8 + \frac{1}{2} \times 6 \right)$$

8 on corners

6 on faces

$$= \frac{4}{3} \pi \left(\frac{\sqrt{2}a}{4} \right)^3 \times 4 = \frac{\pi}{6} \sqrt{2} a^3$$

$$\text{Packing Fraction} = \frac{\pi}{6} \sqrt{2} \approx 0.740$$



(c) sc

$$\text{Maximum radius of the sphere} = \frac{a}{2}$$

$$\text{Volume of spheres} = \frac{4}{3} \pi r^3 \times \left(\frac{1}{8} \times 8 \right)$$

8 on corners

$$= \frac{4}{3} \pi \cdot \left(\frac{a}{2} \right)^3 = \frac{\pi}{6} a^3$$

$$\text{Packing Fraction} = \frac{\pi}{6} \approx 0.524$$

