Electron-Hole Symmetry and Magnetic Coupling in Antiferromagnetic LaOFeAs

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When either electron or hole doped at concentrations $x \sim 0.1$, the LaOFeAs family displays remarkably high temperature superconductivity with T_c up to 55 K. In the most energetically stable $\vec{Q}_M = (\pi, \pi)$ antiferromagnetic (AFM) phase comprised of tetragonal-symmetry breaking alternating chains of aligned spins, there is a deep pseudogap in the Fe 3*d* states centered at the Fermi energy, and very strong magnetophonon coupling is uncovered. Doping (of either sign) beyond $x \sim 0.1$ results in Fe 3*d* heavy mass carriers ($m^* \sim 4 - 8$) with a large Fermi surface. Calculated Fe-Fe transverse exchange couplings $J_{ij}(R)$ reveal that exchange coupling is strongly dependent on the AFM symmetry and Fe-As distance.

Since the appearance of copper oxide high temperature superconductors (HTS) two decades ago,¹ there has been a determined but underfunded effort to discover related superconductors in twodimensional (2D) transition metal oxides (TMO), borides, nitrides, etc. Promising developments in this area include $Li_x NbO_2, [2], Sr_2 RuO_4, [3]$ $Na_x CoO_2$, [4], and $Cu_x TiSe_2$, [5] but all have superconducting critical temperature T_c of 5K or The most striking discovery was that less. of electron-doped hafnium nitride semiconductor (HfNCl) [6] with $T_c = 25$ K. The other distinctive breakthrough,⁷ MgB₂ ($T_c=40$ K), has strong 2D features but contains only s, p elements. Recently, design of possible TMO superconductors has been stimulated by a specific approach outlined by Chaloupka and Khaluillin.⁸

The simmering state of superconductor discovery has been re-ignited by discovery of a new class of layered transition metal pnictides $\mathcal{R}O\mathcal{T}Pn$, where \mathcal{R} is a trivalent rare earth ion, \mathcal{T} is a late transition metal ion, and Pn is a pnictogen atom. The breakthrough of $T_c=26$ K ($T_c^{onset}=32$ K) was reported⁹ for $0.04 \le x \le 0.12$ electron doped $LaO_{1-x}F_x$ FeAs, followed by the demonstration that hole-doping¹⁰ in $La_{1-x}Sr_xOFeAs$, $0.09 \le x \le 0.20$, leads to a similar value of T_c . These values of T_c have now been superseded by the finding that replacement of La by Ce,¹¹ Pr,¹² Nd,¹³ Sm,^{14,15} and Gd¹⁶ result in $T_c =$ 41-55 K, substantially higher than in any materials except for the cuprate HTS.

The transport, magnetic, and superconducting properties of $LaO_{1-x}F_xFeAs$ depend strongly on doping.^{9,10,17} Most interestingly, a kink is observed¹¹ in the resistivity of the stoichiometric ("undoped"



FIG. 1: (color online) The Q_M antiferromagnetic structure of LaOFeAs, with different shades of Fe atoms (top and bottoms planes) denoting the opposing directions of spins in the Q_M AFM phase. Fe atoms lie on a square sublattice coordinated tetrahedrally by As atoms, separated by LaO layers (center of figure) of similar structure. The dashed lines indicate the nonmagnetic primitive cell.

but conducting) compound, which has been identified with the onset of antiferromagnetism (AFM). As a result, the original focus on the nonmagnetic LaOFeAs compound switched to an AFM ground state, in which the two Fe atoms in the primitive cell have oppositely oriented moments. Due to the structure of the FeAs layer, shown in Fig. 1, that requires two Fe atoms in the primitive cell, this ordering represents a Q=0 AFM state.

The basic electronic structure of this class of compounds was presented for LaOFeP, superconducting

at 5 K [18], by Lebègue.¹⁹ The electronic structure of paramagnetic LaOFeAs is similar, and its (actual or incipient) magnetic instabilities have been described by Singh and Du,²⁰ who found that the Fermi level (E_F) lies on the edge of a peak in the density of states (DOS), making the electronic structure strongly electron-hole asymmetric. The Fermi surfaces are dominated by zone center and zone corner cylinders, which underlie several models of both magnetic²¹ and superconducting.^{22,23,24,25} properties. Cao *et al.*²⁶ and Ma and Lu²⁷ demonstrated that a Q=0 AFM state (mentioned above) is energetically favored, but coincidentally (because the electronic structure is substantially different) still leaves E_F on the edge of a DOS peak, *i.e.* strongly particle-hole asymmetric. In both paramagnetic and Q = 0 AFM states a degenerate d_{xz}, d_{yz} pair of Fe orbitals remains roughly half-filled, suggesting possible spontaneous symmetry breaking to eliminate the degeneracy.^{21,28} Such degeneracies have attracted attention in transition metal oxides.²⁹

Subsequently it was reported by Dong *et al.*³⁰ that a $\vec{Q}_M = (\pi, \pi, 0) \sqrt{2} \times \sqrt{2}$ AFM state lies substantially lower still in energy. The spin arrangement consists of Fe chains of aligned spins along one direction (which we take to be the *x*-axis) of the square Fe sublattice, with alternate chains having opposite spin direction. This \vec{Q}_M ordering is what might be expected from the (approximate) nesting of Fermi surfaces in the primitive cell, but the calculated moments are large (1.72 μ_B in the Q=0 phase, 1.87 μ_B for Q_M) and thus is far removed from a 'spin density wave' description. Neutron scattering^{31,32} and x-ray scattering³² have confirmed this in-plane ordering, and reveal that alternating planes of Fe spins are antialigned, *i.e.* the true ordering is (π, π, π) .

To prepare for studying the superconducting state, it is necessary first to understand the normal state from which it emerges. Here we analyze the conducting Q_M AFM phase, using results from two all-electron, full potential codes Wien2k³³ and FPLO^{34,35} using the generalized gradient approximation³⁶ (GGA) functional. We find the Q_M phase to be energetically favored over the Q=0 AFM phase by ~ 75 meV/Fe, which itself lies 87 meV/Fe below the nonmagnetic phase. This energy difference is large enough that neither the Q=0AFM, nor the nonmagnetic, phase will be thermally accessible at temperatures of interest. We neglect the antialignment of spins on the well separated adjacent FeAs layers, which will have little effect on the electronic and magnetic structure of a layer due to the weak interlayer hopping. In either AFM phase,



total DOS (states/eV/spin per cell)

eV/spin per atom)

4

15

FIG. 2: (color online) Top panel: total DOS for the Q_M AFM phase. Bottom panel: spin resolved Fe 3d DOS, showing majority filled and minority half-filled up to the pseudogap, and the As 4p DOS.



FIG. 3: Band structure of the \vec{Q}_M AFM phase along high symmetry directions. Note that two dispersive bands and one narrow band cross E_F along Γ -Y, while only the one flatter band crosses E_F (very near k=0) along Γ -X.

the Fe majority states are completely filled, thus the moment is determined by the occupation of the minority states. From the projected Fe 3d density of states (DOS) shown in Fig. 2, the minority states are almost exactly half-filled, giving 7.5 3d electrons and thus an Fe state that is no more than 0.5e from neutral. While the center of gravity of As 4p weight lies below that of Fe 3p bands, there is strong mixing of these two characters on both sides of E_F , and the As 4p states are certainly unfilled.

Notably, the band structure and DOS is character-

ized by a pseudogap straddling E_F , closing only in a small region along the $\Gamma\text{-}Y$ line near $\Gamma.$ Since the moments, and hence the exchange energies, of the two AFM phases are very similar, the energy gain in the Q_M phase can be ascribed to the formation of the pseudogap. The system could be considered as metallic rather than semimetallic, in the sense that there are two dispersive bands crossing E_F along Γ -Y. One is 1.3 eV wide, comprised of Fe d_{xy} + As p_z character, the other of d_{yz} character is 0.9 eV wide. A third narrower (0.4 eV) band of $3d_{x^2-y^2}$ character crosses E_F near Γ . The crossing of the dispersive bands along Γ -Y are such as to leave only two small distinct 2D Fermi surfaces, shown in Fig. 4: an elliptical hole cylinder at Γ containing ~0.03 holes, and two symmetrically placed near-circular electron tubes midway along the Γ -Y axis. In the sense that the Fermi surfaces are small, the state is semimetallic. The bands near E_F have k_z dispersion of no more than 25 meV.

The d_{xz}, d_{yz} degeneracy is broken by the chains of aligned Fe spins in the Q_M phase. The rough characterization for the minority Fe orbitals is that d_{z^2} and $d_{x^2-y^2}$ states are partially filled, d_{xy} and d_{xz} states are empty, the d_{yz} states are mostly filled but giving rise to the hole Fermi surfaces. (Note that here the x - y coordinate system is rotated by 45° from that usually used for the primitive cell, see Fig. 1.)

A strikingly feature, crucial for accounting for observations, is that the DOS is (roughly) particle-hole symmetric, as is the observed superconducting behavior. All bands near E_F are essentially 2D, resulting in only slightly smeared 2D-like DOS discontinuities at the band edges with structure elsewhere due to band crossings and non-parabolic regions of the bands. The DOS has roughly a constant value of 0.25 states/(eV Fe spin) within 0.15-0.2 eV of E_F , with much flatter bands beyond. The hole and electron effective in-plane masses, obtained from N(E) = $m^*/(\pi\hbar^2)$ for each pocket, are $m_h^* = 0.33, m_e^* = 0.25$. An analogous band structure occurs in electron-doped HfNCl,³⁷ but there superconductivity appears before the heavy bands are occupied.

There are somewhat conflicting indications of the possible importance of electron-phonon coupling in this compound.^{38,39} Fig. 5 provides evidence of strong *magneto*phonon coupling: increase of the As height which changes the Fe-As distance affects the Fe moment at a rate of 6.8 $\mu_B/Å$, indicating an unusually large sensitivity to the Fe-As separation. Fig. 5 also reveals another important aspect: LDA



FIG. 4: (color online) Fermi surfaces of LaOFeAs. (A) and (B): the hole cylinders and electron tubes of the stoichiometric Q_M phase. (C) and (D): hole- and electrondoped surfaces.

and GGA are almost 0.1 Å off in predicting the height of the As layer relative to Fe, a discrepancy that is uncomfortable large. Neglecting the Fe magnetism increases the discrepancy.

"Doping" (change of charge in the FeAs layers) is observed to cause the Néel temperature to decrease, and no magnetic order is apparent in superconducting samples. The effect of (rigid band or virtual crystal) doping on the Q_M electronic structure, either by electrons or holes, is to move E_F into a region of heavier carriers, by roughly a factor of 20 $(m_h^* \sim 6 \sim m_e^*)$. About 0.1 carriers is sufficient to do this, which is just the amount of doping that results in superconductivity. The Fermi surfaces evolve accordingly as shown in Fig. 4: for electron doping the hole cylinder disappears, the electron tubes enlarge and merge; for hole doping the electron tubes decrease in size as the hole cylinder grows and distorts into a diamond-shaped cross section.

The spectrum of magnetic fluctuations is an important property of any AFM phase, and may bear strongly on the emergence of superconductivity. We have calculated from linear response theory the exchange couplings $J_{ij}(q)$ for all pairs $\{i,j\}$ within the unit cell, and by Fourier transform the real space exchange couplings $J_{ij}(R)$, for the transverse spin-



FIG. 5: (color online) The magnitude of the Fe magnetic moment, the change in energy, and the Fe-As distance, as the As height z_{As} is varied.

wave Hamiltonian^{40,41}

$$H = -\sum_{\langle i,j \rangle} J_{ij} \hat{e}_i \cdot \hat{e}_j; \quad J_{ij}(R) = -\frac{d^2 E[\{\theta\}]}{\partial \theta_i(0) \partial \theta_j(R)}, (1)$$

where $\theta_j(R)$ is the angle of the moment (with direction \hat{e}_j) of the *j*-th spin in the unit cell at *R*. For the Q_M AFM phase and experimental structural parameters, the 1st and 2nd neighbor couplings are (distinguishing parallel and perpendicular spins)

$$J_1^{\perp} = -550 \text{ K}; J_1^{\parallel} = +80 \text{ K}; J_2^{\perp} = -260 \text{ K}.$$
 (2)

For comparison, the nearest neighbor coupling^{40,41} in elemental FM Fe is $J_1 \approx 1850$ K, *i.e.* 3-4 times as strong. The signs are all supportive of the actual ordering, there is no frustration. The factor-of-7 difference between the two 1st neighbor couplings reflects the strong asymmetry between the x- and y-directions in the Q_M phase, which is also clear from the bands. The sensitivity to the Fe-As distance is strong: for z(As)=0.635, where the moment is decreased by 40% (Fig. 5), the couplings change by roughly a factor of two: $J_1^{\perp} = -200 \text{ K}, J_1^{\parallel}$ $= +130 \text{ K}, J_2^{\perp} = -140 \text{ K}$. The interlayer exchange constants will be much smaller and, although important for the (three dimensional) ordering, that coupling should leave the spin-wave spectrum nearly two-dimensional.

We emphasize that these exchange couplings apply only to small rotations of the moment (spin waves). The Q=0 phase couplings are different from those for the Q_M phase; furthermore, when FM alignment is enforced the magnetism disappears entirely. The magnetic coupling is phase-dependent, largely itinerant, and as mentioned above, it is sensitive to the Fe-As distance.

The electronic and magnetic structure, and the strength of magnetic coupling, in the reference state of the new iron arsenide superconductors has been presented here, and the origin of the electron-hole symmetry of superconductivity has been clarified. The dependence of the Fe moment on the environment, and an unusually strong magnetophonon coupling, raises the possibility that magnetic fluctuations are involved in pairing, but that it is longitudinal fluctuations that are important here.

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