Electronic and structural properties of La₃Ni₂B₂N₃

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La₃Ni₂B₂N₃ is determined, using local-density-approximation calculations, to be a three-dimensional metal, similar to LuNi₂B₂C and related borocarbides. The band structure shows four hybridized bands crossing the Fermi energy, \( E_F \). The Fermi-surface velocities in the x and z directions are 2.9 \times 10^4 \text{ cm/s} and 1.5 \times 10^4 \text{ cm/s}, respectively, i.e., a 2:1 ratio. This three-dimensional character is due to the open-shell character of the La ions and resulting participation of La orbitals in the states at \( E_F \). The dominant La contribution at \( E_F \) comes from La 5d orbitals, particularly for the outer La layers; La 4f contributions are weaker, but significant. There is a pronounced peak in the density of states occurring near \( E_F \) due to a flat band, though this peak is somewhat smeared on the high-energy side as compared to the corresponding peak in LuNi₂B₂C. Internal structural coordinates and the corresponding optical Raman phonon frequencies have been calculated using force methods.

The discovery of superconductivity in Ni, Pd, and Pt rare-earth borocarbides, with critical temperatures, \( T_c \) as high as 23 K has renewed interest in superconducting intermetallics. In particular, the rapid discovery of \( T_c \) essentially tying the record high \( T_c \) for an intermetallic, the presence of elements frequently associated with magnetism, and the anisotropic, layered crystal structures, all suggested that the superconductivity might be unconventional in analogy with the high \( T_c \) cuprates. This then leads to the expectation that much higher values of \( T_c \) may yet be discovered in these or related compounds.

Electronic structure calculations have, however, shown that despite the layered structures the materials have many similarities to previous families of intermetallic superconductors. Particularly striking is the fact that although the crystal structures are apparently very anisotropic, the electronic structure near the Fermi energy, \( E_F \), is dominated by quite three-dimensional bands with nearly isotropic Fermi surface properties. Based on this as well as evidence for strong electron phonon couplings and other features analogous to other families of materials, such as a high electronic density of states (DOS) at \( E_F \), \( N(E_F) \), it has been concluded that the materials are just conventional strong coupling superconductors, and that as a result it is unlikely that \( T_c \)'s much higher than the old record of 23 K will be discovered in these compounds.

Recently, however, Cava et al. have reported superconductivity with a critical temperature of 12–13 K in an apparently related intermetallic, La₃Ni₂B₂N₃, with a crystal structure much more suggestive of two-dimensional behavior. In particular, like YNi₂B₂C, which has the highest \( T_c \), the crystal structure contains Ni-B sheets consisting of coplanar Ni atoms closely coordinated by B atoms lying above and below the layer. In YNi₂B₂C and the other materials in the family these Ni-B sheets are separated by a single Y (or other trivalent metal) carbide layer. The three dimensionality of the electronic structure near \( E_F \) is due to coupling through these Y-C layers. In La₃Ni₂B₂N₃, this layer is replaced by three rock salt La-N layers. This has led to the expected of a strongly two-dimensional electronic structure, first of all due to the larger separation between the Ni-B sheets, and second because of the likelihood that the rocksalt La-N trilayers between them are ionic and insulating or nearly insulating. This expectation is, however, open to question, since the superconductivity in these materials is thought to be related to a peak in the electronic DOS near \( E_F \); insulating LaN is expected to have a net charge close to zero, presumably giving a different band filling and DOS peak position than a YC or LaC layer. Further, it has been shown for LuNi₂B₂C, that the peak structure near \( E_F \) does not occur for an isolated Ni-B sheet, but is dependent on interactions involving the Lu and C atoms as well. In the discussion that follows, we use LuNi₂B₂C as an example of this family of borocarbide superconductors since its behavior seems to be generic.

Here we report density functional calculations of the electronic structure of La₃Ni₂B₂N₃ elucidating the relationship of this material with the borocarbide superconductors. We find the unexpected result that the LaN layers are metallic with open shell La atoms and that as a result La₃Ni₂B₂N₃ is quite three dimensional. In order to perform these calculations it was necessary to relax the three, presently unknown, internal structural parameters, using total energy and force methods. This also yielded the three corresponding \( \Gamma \) point Raman phonon frequencies.

The calculations were performed self-consistently, within the local density approximation (LDA), as parametrized by Hedin and Lundqvist using the general potential linearized augmented plane wave (LAPW) method. Well converged basis sets consisting of approximately 2025 functions were used. The zone integrations were based on a set of 20 special points in the irreducible wedge during the iterations to self-consistency. For the density of states (DOS), 77 points in the wedge were used. The high lying extended La 5p and 5s states were treated as valence states using a local orbital extension. The Raman frequencies and internal structural parameters, corresponding to the B and outer layer La and N heights, were computed from the variation of the atomic forces with structure. These forces were determined using the method of Yu, Singh, and Krakauer. The lattice parameters were fixed at their experimental values.
The heights of the B and outer La and N atoms were found to be $z_B = 0.199$, $z_{La} = 0.131$, and $z_{N} = 0.128$ in units of the e lattice parameter (20.516 Å) and with the inner La-N layer at $z = 0$. The calculated fully symmetric $A_{1g}$ Raman vibrations are almost pure La mode at 106 cm$^{-1}$, and two strongly mixed B,N modes at 323 cm$^{-1}$ and 896 cm$^{-1}$ where the upper mode has adjacent B and N atoms moving against each other. Both of these modes produce distortions of the NiB$_2$ tetrahedra similar to those of the $A_{1g}$ mode in LuNi$_2$B$_2$C. Mattheiss, Siegrist, and Cava have suggested that the superconductivity in the borocarbides is due to a strong coupling of such modes to electrons at the Fermi energy. The highest mode (896 cm$^{-1}$) is at a 5% higher frequency than the corresponding $A_{1g}$ mode in LuNi$_2$B$_2$C [calculated at 850 cm$^{-1}$ (Ref. 6)]. This is not entirely unexpected since some increase in the highest frequency is expected due to the greater number of the degrees of freedom due to outer layer N motions.

The band structure and corresponding total and atom projected DOS of La$_3$Ni$_2$B$_2$N$_3$ with the equilibrium atomic positions are shown in Figs. 1 and 2, respectively. Both similarities and significant differences from the electronic structure of the borocarbides are evident, but the differences seem to be more matters of detail. First of all, and perhaps most importantly, contrary to expectations of near two-dimensional character, the electronic structure near $E_F$ derives from several bands with strong $c$-axis dispersions. The Fermi surface velocities, $\langle v_F \rangle^1/2$ and $\langle v_F^2 \rangle^1/2$, where $\langle \rangle$ denotes an average over the Fermi surface, are $2.92 \times 10^5$ cm/s and $1.48 \times 10^5$ cm/s. This gives a ratio $v_F:u_F$ of 2:1 as compared to roughly 1:1 in LuNi$_2$B$_2$C. The four bands that cross the Fermi energy yield large sheets of Fermi surface, as in the borocarbides; two large sheets have crossings in the $c$-axis direction. Thus the electronic structure of La$_3$Ni$_2$B$_2$N$_3$ is not in any sense two dimensional. This may be understood in terms of the DOS (Fig. 2).

The most prominent feature of the DOS about $E_F$ is the presence of a peak, split off from the high side of the Ni d bands, similar to LuNi$_2$B$_2$C, for example. This peak has significant contributions from hybridization with the B atoms and also has significant contributions from the two outer La atoms, which are in proximity to the Ni-B sheets and remarkably the inner La atoms, as well. These La contributions have both 5$d$ and 4$f$ characters and are largest on the high-energy side of the peak, contributing to an extended tail, which is not present in LuNi$_2$B$_2$C. Clearly, the La atoms are open shell and only partially ionized, with the result that the La-N trilayer is metallic.

The inner layer N 1$s$ core level is shifted to 0.055 Ry lower binding energy than the outer layer N 1$s$ level. The inner layer La deep core levels are also shifted to lower binding energy relative to the outer La, by 0.024 Ry. This and the upward shift of the inner layer N 2$p$ derived DOS all imply that the La-N layers, particularly the outer layers, have a significant net negative charge. Integration of the DOS projections gives a crude estimate of 0.5 extra electrons per outer layer.

For La$_3$Ni$_2$B$_2$N$_3$ ($T_c = 13$ K), we calculate $N(E_F) = 5.7$ Ry$^{-1}$ on a per formula unit basis. This may be compared with 65.3 Ry$^{-1}$ in LuNi$_2$B$_2$C ($T_c = 17$ K) (Ref. 6) and 33.9 Ry$^{-1}$ in LaPt$_2$BC ($T_c = 11$ K). The Drude plasma energies,
$h\Omega_{p,\mu} = \left[ 4 \pi e^2 N(E_F) \langle v_\mu^2 \rangle / V_c \right]^{1/2}$, where $V_c$ is the cell volume, are 4.4 eV and 2.3 eV in the $x$ and $z$ directions, respectively. This corresponds to a BCS clean limit London penetration depth ($\lambda = c/\Omega_p$) of 450 Å normal to $c$.

The main La $4f$ peaks are approximately 3 eV above $E_F$. At $E_F$ the La $5d$ contribution is approximately three times larger than the La $4f$ contribution for the outer La atoms, but these are roughly equal for the inner La atom due to a smaller $5d$ contribution. The N $2p$ contributions to $N(E_F)$ are significant and arise from both the inner and outer layer N atoms; the inner N atom has only a slightly lower contribution than an outer layer N. However, besides the La-N interactions that this implies, there are strong covalent interactions both between the Ni and B atoms and between the outer N and Ni atoms as evidenced by the similar shape of their DOS projections from $-0.6$ to $-0.2$ Ry relative to $E_F$ as well as above the La $4f$ peak. The inner layer N atoms have a much more compact $2p$ DOS reflecting the absence of Ni neighbors.

As mentioned, Mattheiss, Siegrist, and Cava have associated the superconductivity of the borocarbides with the presence of a flat band near $E_F$, which gives rise to the DOS peak and changes in its occupation due to strong $\Delta_{1g}$ phonon coupling with $s$-$p$ derived bands also near the Fermi energy. The coupling is ascribed to modulation of bond angles in the NiB$_3$ tetrahedra. In LuNi$_2$B$_2$C this flat Ni $d$ derived band is just above $E_F$ along most of the $\Gamma$-$110$ line (see the caption of Fig. 1). In La$_3$Ni$_2$B$_2$N$_3$ a similar flat band occurs, but it is shifted to 300 meV below $E_F$ along $\Gamma$-$110$ and acquires a considerably larger dispersion along this line. The flat Ni $d$ derived section that gives rise to the DOS peak occurs rather along almost the whole $Z$-$111$ line.

In LuNi$_2$B$_2$C, there are also predominantly $s$-$p$ derived bands near the Fermi energy in La$_3$Ni$_2$B$_2$N$_3$. Examples are the two bands that disperse upwards through $E_F$ along $\Gamma$-$100$, originating from $\Gamma$ as a doubly degenerate state at $-0.5$ eV. This band at $\Gamma$ is predominantly B $2p$ and outer layer N $2p$ derived. It also has La $5d$ character involving both the inner and outer layer La atoms, as well as some Ni $3d$ character. We have investigated the coupling of $\Delta_{1g}$ phonons to this state by calculating the electronic structure including B displacements of 0.04 Å (with additional outer layer N displacements) as in the 323 cm$^{-1}$ and 896 cm$^{-1}$ modes. These involve the same distortion of the NiB$_3$ tetrahedra, but different modulations of the B-N and Ni-N bonds. For the higher frequency mode, this $\Gamma$ point $s$-$p$ band is shifted relative to $E_F$ by 0.01 Ry (downwards for B motion towards the Ni), corresponding to a “deformation potential” of about 3 eV/Å. Similar, but generally smaller effects on the $s$-$p$ bands near $E_F$ occur throughout the zone. This is about half of the maximum value found by Mattheiss, Siegrist, and Cava for LuNi$_2$B$_2$C.

On the other hand, with displacements corresponding to the 323 cm$^{-1}$ mode, we find much smaller deformation potentials. For the actual crystal structure, the DOS peak near $E_F$ occurs at $-29$ meV (relative to $E_F$). With the frozen in 896 cm$^{-1}$ pattern (0.04 Å), it occurs at $+99$ meV (i.e., a shift of 128 meV), while with the 323 cm$^{-1}$ pattern (0.04 Å) it occurs at $-27$ meV (shift of 2 meV). As mentioned, both the 323 cm$^{-1}$ and 896 cm$^{-1}$ modes involve the same distortion of the NiB$_3$ tetrahedra; the main difference is that the 896 cm$^{-1}$ mode modulates the outer layer N-B bond lengths, while the 323 cm$^{-1}$ mode does not since it involves in phase motions of the adjacent B and N atoms. (Note also that the phase of the outer layer N-Ni motions and Ni-B motions is shifted by $\pi$.) Thus the coupling of these optical phonons is due to modulation of B-N bond lengths as opposed to angles in the NiB$_3$ tetrahedra.

In summary, we find that La$_3$Ni$_2$B$_2$N$_3$ fits in very well with the picture provided by previous calculations for the borocarbide superconductors like LuNi$_2$B$_2$C, and should be regarded as just another member of this class. In particular, there is no near two dimensionality of the electronic structure evident near $E_F$. The implication is that while this and other modifications of the borocarbide superconductors may be very important in tailoring their properties, such changes are unlikely to lead to dramatically higher critical temperatures, as in the high critical temperature cuprates.

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LAPW sphere radii of 2.2, 1.9, 1.3, and 1.3 a.u. were used for La, Ni, N, and B, respectively.


Due to the body centering and inversion center, atoms occur at heights \( \pm z \) and \( 0.5 \pm z \).

In order to simplify the analysis of the electron phonon coupling, idealized patterns for the upper two modes were used. These consisted, for the 323 cm\(^{-1}\) mode of equal in-phase displacements of adjacent B and N atoms, and for the 896 cm\(^{-1}\) mode of equal out-of-phase displacements. The calculated phonon polarization vectors (order: La,N,B) are \((-0.99, -0.10, -0.08),\)
\((-0.13, 0.69, 0.72),\) and \((-0.02, 0.72, -0.69)\) in order of increasing frequency. Taking the masses into account, the actual ratios of N to B displacements in the upper two modes are 0.8 and \(-0.9\) for the upper two modes.